

# 1 Overview

## 1.1 Units

Throughout these lectures I will use natural units <sup>1</sup>

$$c = 8\pi G = \hbar = 1 \quad (1)$$

Occasionally, I will reintroduce some units for clarity, for emphasis, or to follow standard conventions. I define the Planck mass as

$$M_{\text{Pl}} \equiv \left( \frac{\hbar c}{8\pi G} \right)^{1/2} = 4 \mu\text{g} \quad (2)$$

The Planck length and time are defined similarly and are extremely small.

The standard units of high energy physics are to set  $c = \hbar = 1$  and use the giga electron volt or GeV as the remaining dimensional parameter. In these units, the mass of an electron is

$$m_e = 5 \times 10^{-4} \text{ GeV} \quad (3)$$

The mass of a proton or neutron is

$$m_p \simeq m_n = 0.9 \text{ GeV} \quad (4)$$

The scale of electro-weak symmetry breaking is

$$m_{\text{EW}} \sim 10^2 \text{ GeV} \quad (5)$$

The Planck mass is

$$M_{\text{Pl}} = 2.436 \times 10^{18} \text{ GeV} = 9 \times 10^4 \text{ kcal} \quad (6)$$

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<sup>1</sup>Note that many authors instead choose to set  $G = 1$ .

The standard units of the late universe are megaparsecs or Mpc for length

$$\text{pc} = 3.3 \text{ c yr} \quad (7)$$

$$\text{Mpc} = 1.6 \times 10^{38} \text{ GeV}^{-1} = 3.8 \times 10^{56} \quad (8)$$

km s<sup>-1</sup> for velocity

$$\text{km s}^{-1} = 3.3 \times 10^{-6} \quad (9)$$

years for time

$$\text{yr} = 4.8 \times 10^{31} \text{ GeV}^{-1} = 1.2 \times 10^{50} \quad (10)$$

and solar masses for mass

$$M_{\odot} = 1.1 \times 10^{57} \text{ GeV} = 4.6 \times 10^{38} \quad (11)$$

## 1.2 Basic observed properties of the universe

1. The universe is **old**.

The oldest objects in the universe whose age has been estimated are about  $10^{10}$  years old.

$$T_0 \gtrsim 10^{10} \text{ yr} \sim 10^{60} \quad (12)$$

2. The universe is **big**.

No observable boundary or periodicity.

$$L_0 \gtrsim 10^{10} c \text{ yr} \sim 10^{60} \quad (13)$$

3. There is a **lot of matter** in the universe.

$$M_0 \gtrsim 10^{21} M_\odot \sim 10^{60} \quad (14)$$

4. The universe is approximately **homogeneous** and **isotropic** on the largest observable scales.

5. The observable universe is **expanding**.

The expansion rate is given by the Hubble parameter  $H$ . The current value of the Hubble parameter is

$$H_0 \simeq 65 \text{ km s}^{-1} \text{ Mpc}^{-1} \quad (15)$$

$$\sim \frac{1}{10^{10} \text{ yr}} \sim 10^{-42} \text{ GeV} \sim 10^{-60} \quad (16)$$

6. The universe is **flat**.

There is no observable large scale spatial curvature.

7. The universe is not exactly homogeneous and isotropic. **Density perturbations** have an amplitude  $\sim 10^{-5}$  and an approximately **scale-invariant** spectrum on the largest observable scales.

8. The matter content of the universe is dominated by **cold dark matter** with about 15% ordinary matter.

$$\rho_{\text{CDM}} \simeq 6\rho_{\text{B}} \quad (17)$$

9. The **baryon**<sup>2</sup> to cosmic microwave background **photon ratio** is about  $5 \times 10^{-10}$ .

$$n_\gamma \simeq 2 \times 10^9 n_{\text{B}} \quad (18)$$

10. The current temperature of the **cosmic microwave background radiation** is

$$T_{\gamma 0} = 2.73 \text{ K} = 2.35 \times 10^{-4} \text{ eV} \quad (19)$$

which corresponds to a photon number density

$$n_{\gamma 0} = 0.41 \text{ mm}^{-3} \quad (20)$$

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<sup>2</sup>A baryon is a particle made of three quarks, for example, a proton or neutron. At energies below the electro-weak scale, the number of baryons is conserved to a very good approximation.